

December 5, 1942

Dear Dr Discombe,

Yes, as you thought, your problem is quite a straightforward one, though a little confusing owing to the factors which enter into it, e.g., the number of leucocytes is estimated to be  $\underline{n}$ , but this is based on a count, not of  $\underline{n}$  but of  $\underline{a}$  cells observed in the haemocytometer. The variance of  $\underline{a}$  is  $\underline{a}$ , so the variance of  $\underline{n}$  is

$$\frac{\underline{n}^2}{\underline{a}^2} \times \underline{a} = \frac{\underline{n}^2}{\underline{a}}$$

and the variance of  $\log \underline{n}$  is simply  $\frac{1}{\underline{a}}$ .

If  $\underline{p}$  is the proportion of a particular kind of leucocyte observed in a sample of  $\underline{b}$ , then the sampling variance of  $\underline{p}$  is, as is well known,

$$\frac{p(1-p)}{b},$$

so the sampling variance of  $\log \underline{p}$  is

$$\frac{1-p}{pb}.$$

As  $\underline{n}$  and  $\underline{p}$  have been estimated independently, we may now say that the sampling variance of the log of the absolute estimate  $np$  is

$$\frac{1}{a} + \frac{1-p}{pb} .$$

ing  
Multiply this by the square of the estimated  $\underline{np}$  will give the sampling variance of this estimate.

I have set the above out in full, as I thought you would prefer to see the detailed working to my sending you a dogmatic formula, which has the disadvantage that its symbolism may be misunderstood.

Yours sincerely